Fano manifolds and the Lefschetz defect

Cinzia Casagrande¹

 1 (Torino, Italy)

Abstract: We will discuss the geometry of a (smooth, complex) Fano variety X, first introducing the Lefschetz defect and its properties, and then focusing on Fano 4-folds and their birational geometry. The Lefschetz defect $\delta(X)$ is an invariant of X which relates the Picard number of X to that of its prime divisors; it is a nonnegative integer. If $\delta(X) > 3$, then X is a product of a del Pezzo surface with another Fano variety. When $\delta(X) = 3$, X has a fibration in del Pezzo surfaces with a very precise structure. We will discuss these results, that allow to classify completely Fano 4-folds X with $\delta(X) > 2$. Then we will see how birational geometry, together with the Lefschetz defect, can be used to explicitly study and classify Fano 4-folds with large second Betti number b_2 . In particular, when $b_2(X) > 12$, then X is a product of del Pezzo surfaces.