(Dis)continuities of Lyapunov exponents

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Let f be a C^{∞} surface diffeomorphism with positive topological entropy, and let μ_n be a sequence of ergodic invariant measures which converge weak star to an ergodic limiting measure μ with positive entropy.

We show that if the entropies of μ_n converge to the entropy of μ , then the Lyapunov exponents of μ_n converge to the Lyapunov exponents of μ .

If the entropies of μ_n do not converge to the entropy of μ , then the Lyapunov exponents of μ_n may not converge to the Lyapunov exponents of μ . In this case, we relate the discontinuity in entropy to the discontinuity in Lyapunov exponents.

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