Lipschitz continuity of nonnegative minimizers of function of Bernoulli type with nonstandard growth

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I will report on research done in collaboration with Claudia Lederman from the University of Buenos Aires on the Lipschitz continuity of nonnegative minimizers to functionals

$$J(u) = \int_{\Omega} F(x, u(x)\nabla u(x)) + \lambda(x)\chi_{\{u>0\}}dx.$$

Here $F(x, s, \eta)$ is a function of p(x)-type growth with p Lipschitz continuous, and $0 \le \lambda_1 \le \lambda(x) \le \lambda_2 < \infty$.

For example, we may take $F(x, s, \eta) = a(x, s)|\eta|^{p(x)} + b(x)|s|^{p^*(x)}$, $0 \leq b(x) \in L^{\infty}$, $0 < a_0 \leq a(x) \leq a_1 < \infty$ satisfying some suitable assumptions. Also, $F(x, s, \eta) = G(|\eta|^{p(x)}) + f(x, s)$ with G strictly convex and suitable f. Here, $p^* = \frac{Np(x)}{N-p(x)}$ when $\max_{\Omega} p < N$.