Regularity estimates for fully nonlinear unbalanced degenerate models

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In this Talk we will establish sharp $C_{\text{loc}}^{1,\beta}$ regularity estimates for bounded solutions of a class of fully nonlinear elliptic PDEs with unbalanced degeneracy, whose model equation is given by

$$[|Du|^p + \mathfrak{a}(x)|Du|^q] \mathcal{M}^+_{\lambda,\Lambda}(D^2u) = f(x) \quad \text{in} \quad \Omega,$$

for a bounded domain $\Omega \subset \mathbb{R}^N$, and suitable data $p, q \in (0, \infty)$, $(p < q) \mathfrak{a} \ge 0$ and f. Our approach is based on geometric tangential methods and makes use of a refined oscillation mechanism combined with compactness and scaling techniques. At the end, we present some connections of our findings with a variety of nonlinear problems in the theory of elliptic PDEs, which may have their own mathematical interest. This is a joint work with Gleydson C. Ricarte (UFC-Brazil).