Block theory for profinite groups

John MacQuarrie¹, Ricardo Franquiz Flores¹

 1 UFMG

If k is a field of characteristic p and G is a finite group, the group algebra kG need not be indecomposable as an algebra. The block theoretic approach to the representation theory of kG is to write kG as a direct product of indecomposable algebras – the "blocks" of G – and study the modules for each block separately. To each block B is associated a p-subgroup D, which measures the difficulty of the block. Very little is understood in general, but blocks whose D is cyclic are classified. We explain this theory and extend it to profinite groups.