

Overdetermined elliptic problems in exterior domains.

Pieralberto Sicbaldi ¹

¹ Université d'Aix-Marseille (France) and Universidad de Granada (Spain)

Overdetermined elliptic systems of the form

$$\left\{ \begin{array}{ll} \Delta u + f(u) = 0 & \text{in } \Omega \subset \mathbb{R}^n, n \geq 2 \\ u = 0 & \text{on } \partial\Omega \\ \frac{\partial u}{\partial \vec{n}} = \text{constant} & \text{on } \partial\Omega \end{array} \right.$$

appear in many problems in Physics and Applied Mathematics. In this talk, I will consider overdetermined elliptic systems in exterior domains, i.e. domains that are the complement of a compact region. I will present a symmetry results with classification of solution for the case where the PDE is a Allen-Cahn type equation, and a perturbation results with the construction of new solutions in the case where the PDE is the Nonlinear Schroedinger equation.