Yann Bugeaud. Around the Littlewood conjecture.

Abstract. The Littlewood conjecture in diophantine approximations claims that every pair (α, β) of real numbers satisfies

$$\inf_{q\geq 1} q \|q\alpha\| \|q\beta\| = 0$$

where $\|\cdot\|$ denotes the distance to the nearest integer. In 2004, de Mathan and Teulié asked the following analogous question: for a given prime number p, is it true that

$$\inf_{q\geq 1} q \|q\alpha\| |q|_p = 0$$

holds for every real number α ? Here, $|\cdot|_p$ denotes the *p*-adic absolute value normalized such that $|p|_p = p^{-1}$. We present recent results towards the resolution of these two problems, which are still not solved.