SIMPLE MODELS OF STRINGS OF CHARACTERS WITH INFINITE ALPHABET WITH APPLICATIONS TO ORDER BOOK DYNAMICS

Helder Rojas¹, Anatoly Yambartsev²,

¹Department of Statistics Institute of Statistics and Mathematics University of São Paulo helderrm@ime.usp.br

²Department of Statistics Institute of Statistics and Mathematics University of São Paulo yambar@gmail.com

Abstract

We consider the a family of Markov chains defined on the sequences of characters (strings, or words) with infinite alphabet. For some examples inspired by the models of high frequency trading we obtain a conditions for ergodicity, transience and null recurrence. In order to prove this we use the construction of Lyapunov functions techniques.

References

- GAJRAT, V.A. MALYSHEV AND M.V. MENSHIKOV, Classification of Markov Chain Describing the Evolution of Random Strings. [Research Report] RR-2022, 1995, Moscow State University.
- [2] G. FAYOLLE, V.A. MALYSHEV AND M.V. MENSHIKOV, Topics in Constructive Theory of Countable Markov Chain. Cambridge Univ. Press, Cambridge 1993.
- [3] D. VERE- JONES, Ergodic Properties of Nonnegative Matrices-I. Pacific Journal of Mathematics Vol. 22, N.2, 1967. Institute of Advanced Studies Australian National University.