Asymptotic Profiles of The Exclusion Process With Slow Boundary

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Abstract: We study the hydrodynamic behavior of the simple symmetric exclusion process with slow open boundary. In this process, particles describe independent random walks in the space $\{1, \ldots, N-1\}$, using the exclusion rule (which says that two particles cannot occupy the same site at the same time). Particles can also be born or die on the sites 1 and N-1 with rates proportional to $N^{-\theta}$, where θ is a non-negative parameter. In the diffusive scaling, the density of particles converges to the weak solution of a heat equation with boundary conditions that depend on θ : if $\theta \in (0, 1)$, we get Dirichlet boundary condition; if $\theta = 1$, we get Robin boundary condition; if $\theta > 1$, we get Neumann boundary condition. Moreover, the asymptotic profile of stationary measure is proven to be the stationary solution of the hydrodynamic equation.

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