Mariusz Lemańczyk. Automorphisms with quasi-discrete spectrum, multiplicative functions and average orthogonality along short intervals.

Abstract. We show that Sarnak's conjecture on Möbius disjointness holds in every uniquely ergodic model of a quasi-discrete spectrum automorphism. A consequence of this result is that, for each non-constant polynomial $P \in \mathbb{R}[x]$ with irrational leading coefficient and for each multiplicative function $\nu: \mathbb{N} \to \mathbb{C}, \ |\nu| \leq 1$, we have

$$\frac{1}{M} \sum_{M \le m < 2M} \frac{1}{H} \left| \sum_{m \le n < m + H} e^{2\pi i P(n)} \nu(n) \right| \longrightarrow 0.$$

This is my joint work with H. El Abdalauoi and T. de la Rue.