

Instanton sheaves and components of the moduli space of semistable sheaves
on the projective space

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Recent results by Tikhomirov, and by the author and Verbitsky have answered old questions about the geometry of the moduli space $I(c)$ of rank 2 instanton bundles of charge c on the projective space: we now know that this is an irreducible, non-singular affine variety of dimension $8c-3$. The next step is to study its compactification.

Since every rank 2 instanton bundle on P^3 is stable, $I(c)$ can be regarded as an open subset of the Gieseker--Maruyama scheme $M(c)$ of semistable rank 2 torsion free sheaves on P^3 with Chern classes $c_1=c_3=0$ and $c_2=c$. One can then consider the closure of $I(c)$ within $M(c)$.

In this talk we show that the singular locus of non-locally free rank 2 instanton sheaves on P^3 have pure dimension 1. We then describe certain irreducible components of the boundary of $I(c)$ with dimension $8c-4$. Such components consist of stable, non-locally free rank 2 instanton sheaves whose singular loci are rational curves. In addition, we describe new components of $M(3)$ and $M(5)$ consisting of stable, non-locally free rank 2 instanton sheaves whose singular loci are elliptic curves.

The results presented are joint work with M. Gargate and with D. Markushevich and A. S. Tikhomirov.